# Study of Tri-level Neutral Point Clamped Inverter for 3-Phase 3-Wire and 3-Phase 4-Wire Applications 

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#### Abstract

In this paper, the theoretical differences and similarities of Triłevel Neutral-Point-Clamped Inverters in 3-phase 3-wire and 3-phase 4 wire systems are studied. In the past researches, almost all the studies of Tritevel NPC Inverter are focused on the 3 phase 3 wire applications. However, more flexible application strategy can be taken in the Tri-level NPC Inverter Structure. With the connection of neutral wire and mid-point of d. c. linked capacitors of Trilevel inverter, it turns into 3-Phase 4-Wire Operation. In this paper, more detailed discussion is performed. Simulation and experimental results are given accordingly.


Keywords-Power Quality Compensation, Tri-level Inverter, 3 Dimensional Pulse-Width-Modulation

## I. INTRODUCTION

The 3Phase 4Wire Inverter Topology [1] can be mainly classified into 4 -Leg configuration and 3-Leg Center-Split structure. However, according to the past comparisons and discussions of the 2 -Level 3 -Phase 4 Wire Inverters, the $3-L e g$ Center-Split structure has following drawbacks: Complicated Control Strategy, D. C. Linked Voltage Variation and Lower D. C. Voltage Utility Ratio [2]. However, the above conclusion is valid only for 2 Level Inverter Structures, but not the Tri-level Neutral-Point-Clamped system [3]. The convenient and flexible structure can be received if Tri-level NPC Inverter is in applications of 3-Phase 3-Wire and 3-Phase 4-Wire Systems. It is obvious that when a wire is connected between the mid-point of d. c. linked capacitors of Tri-level NPC inverter and the neutral wire of 3-Phase 4-Wire system, Tri-level NPC Inverter is in 3-Phase 4 Wire Operation. Without the neutral wire connection, it turns into a 3-Phase 3-Wire System. No further adaptation of the Tri-level NPC Inverter's circuit configuration is needed. Besides, the d. c. voltage utilization ratios of Trilevel NPC Inverters for 3-Phase 3-Wire and 3-Phase 4 Wire cases will be the same. No matter it is 3 -phase 3 wire or 3-phase 4-wire system, Tri-level NPC Inverter is suffered fromthe d. c. voltage variation issue. Due to the above consideration, Tri-level NPC Inverter may be a good strategy in the applications for 3-Phase 3-Wire and 3-Phase 4Wire Systems. In this paper, the theoretical differences and similarities of Tri-level NPC Inverters in 3 -phase 3 -wire and 3 -phase 4 wire systems are studied. Simulation and experimental results are given accordingly in this paper.

## II. CIRCUIT CONFIGURATION

Fig. 1 shows the structure of Tri-level Neutral Point Clamped Inverter for 3-Phase 3-Wire System. Refering to Fig. 2, a 3-phase 4 wire 2 -level center-split inverter is shown. In Fig.2, a wire is connected between the midpoint of d.c. side and the neutral wire of the system, it turns into a 3 -phase 4 -wire system. However, according to this structure and comparing with 4 arm structure for 3 phase 4 -wire system, the d.c. voltage utility ratio is reduced into half of 4 arm case, and d.c. linked voltage variation is occurred. Based on the above analysis for $2-$ level system, there are a lot of researches [2] focusing on the 4 -arm structure for 3-phase 4 -wire applications.


Fig. 1 Tri-Level NPC Inverter Structure for 3-Phase 3-Wire System


Fig. 2 Two -Level Center-Split 3-Phase 4Wire Inverter


Fig. 3 Tri-level NPC 3-Phase 4_wire Inverter
Further consideration is taken for Tri-level NPC system. It is obvious that when a wire is connected between the mid-point of d. c. linked capacitors of Trilevel NPC inverter and the neutral wire of 3-Phase 4-Wire
system, Tri-level NPC Inverter is in 3-Phase 4-Wire Operation. Fig. 3 shows the circuit configuration of Trilevel NPC 3-Phase 4-Wire System. Furthermore, 3-phase 3 -wire and 3 phase 4 wire systems have the same d.c. voltage utility ratio and d.c. voltage variation issue.

## III. 3-Phase 3-Wire And 3-Phase 4-Wire Control

 Strategies and Their dC Voltage Variation issues
## A. Review of Traditional 3-Phase 3-Wire Tri-level NPC

 InverterIn traditional 3-Phase 3-Wire Tri-Level NPC Inverter, there are totally 27 voltage space vectors, but there are only 19 available switching states. Furthermore, different voltage vector may have different effect on the d.c. voltage variation. Normally, the 3 -level voltage space vectors are divided into 4 groups: Zero, Small, Medium and Large Vectors [3][4][5][6].


Fig. 4 Voltage Space Vector's Allocation in $\alpha \beta$ frame
Fig. 4 shows the 3 -level voltage space vector's allocation in $\alpha \beta$ frame. It may be considered as the basic control scheme, 2-Dimensional PWM. Table 1 summaries the results from [3]~[6] for those available voltage space vectors, switching patterns, vector groups, usable switching states and the d.c. voltage variation. In Table 1, the symbol " N " means that there is no effect on the d.c. voltage variation. Obviously, the vectors $\left\{\vec{V}_{000}, \vec{V}_{00 p}, \vec{V}_{00 n}\right\}$ do not have any influence on the d.c. voltage variation of the inverter, and they are belonged to the same group as the same available state. However, the influence of the medium vectors $\left\{\vec{V}_{12}, \vec{V}_{23}, \bar{V}_{34}, \vec{V}_{45}, \vec{V}_{56}, \vec{V}_{61}\right\}$ on the d.c. voltage variation are unknown and it depends on the connected loads and whether those 3 phase loads are balanced or not. If the connected loads on 3 phases are unknown or unpredictable, there is no way to use those vectors to control the d.c. voltage variation. Nevertheless, in small vector group, when the vector of $\left\{\vec{V}_{01 p}, \vec{V}_{02 p}, \vec{V}_{03 p}\right.$, $\left.\vec{V}_{04 p}, \vec{V}_{05 p}, \vec{V}_{06 p}\right\}$ is chosen, the upper d.c. side linked voltage is decreased and vice versa. By reasonable
choosing of switching vector from small-vector group, the d.c. voltage variation can be controlled.

TABLE 1
SUMMARY OF 3-LEVEL NPC 3-PHASE 3-WIRE INVERTER

| Vector <br> Number | Voltage <br> Space <br> Vector | Switching <br> Patterns | Group | Available <br> State | DC <br> Voltage <br> Variation |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 1 | $\bar{V}_{000}$ | $\{0,0,0\}$ | Zero | 1 | N |
| 2 | $\bar{V}_{00 p}$ | $\{1,1,1\}$ | Zero | 1 | N |
| 3 | $\bar{V}_{00 n}$ | $\{-1,-1,-1\}$ | Zero | 1 | N |
| 4 | $\vec{V}_{1}$ | $\{1,-1,-1\}$ | Large | 2 | N |
| 5 | $\vec{V}_{2}$ | $\{1,1,-1\}$ | Large | 3 | N |
| 6 | $\vec{V}_{3}$ | $\{-1,1,-1\}$ | Large | 4 | N |
| 7 | $\vec{V}_{4}$ | $\{-1,1,1\}$ | Large | 5 | N |
| 8 | $\vec{V}_{5}$ | $\{-1,-1,1\}$ | Large | 6 | N |
| 9 | $\vec{V}_{6}$ | $\{1,-1,1\}$ | Large | 7 | N |
| 10 | $\bar{V}_{12}$ | $\{1,0,-1\}$ | Medium | 8 | unknown |
| 11 | $\bar{V}_{23}$ | $\{0,1,-1\}$ | Medium | 9 | unknown |
| 12 | $\vec{V}_{34}$ | $\{-1,1,0\}$ | Medium | 10 | unknown |
| 13 | $\bar{V}_{45}$ | $\{-1,0,1\}$ | Medium | 11 | unknown |
| 14 | $\vec{V}_{56}$ | $\{0,-1,1\}$ | Medium | 12 | unknown |
| 15 | $\vec{V}_{61}$ | $\{1,-1,0\}$ | Medium | 13 | unknown |
| 16 | $\vec{V}_{01 p}$ | $\{1,0,0\}$ | Small | 14 | Upper <br> Decrease |
| 17 | $\vec{V}_{0 n}$ | $\{0,-1,-1\}$ | Small | 14 | Lower <br> Decrease |
| 18 | $\vec{V}_{02 p}$ | $\{1,1,0\}$ | Small | 15 | Upper <br> Decrease |
| 19 | $\vec{V}_{02 n}$ | $\{0,0,-1\}$ | Small | 15 | Lower <br> Decrease |
| 20 | $\vec{V}_{03 p}$ | $\{0,1,0\}$ | Small | 16 | Upper <br> Decrease |
| 21 | $\vec{V}_{03 n}$ | $\{-1,0,-1\}$ | Small | 16 | Lower <br> Decrease |
| 22 | $\vec{V}_{04 p}$ | $\{0,1,1\}$ | Small | 17 | Upper <br> Decrease |
| 23 | $\vec{V}_{04 n}$ | $\{-1,0,0\}$ | Small | 17 | Lower <br> Decrease |
| 24 | $\vec{V}_{05 p}$ | $\{0,0,1\}$ | Snall | 18 | Upper <br> Decrease |
| 25 | $\vec{V}_{05 n}$ | $\{-1,-1,0\}$ | Small | 18 | Lower <br> Decrease |
| 26 | $\vec{V}_{06 p}$ | $\{1,0,1\}$ | Small | 19 | Upper <br> Decrease |
| 27 | $\vec{V}_{00 n}$ | $\{0,-1,0\}$ | Small | 19 | Lower <br> Decrease |

## B. Study of Tri-level NPC 3-Phase 4-Wire Inverter

According to circuit configuration of 2-Level CenterSplit Inverter in Fig. 2, it is obvious that the Tri-level NPC inverter can be classified as one of the Center-Split Inverters so that only a wire is connected with the neutral ground of 3-Phase 4-Wire System from the mid-point of Tri-level NPC Inverter as shown in Fig. 3. The Tri-Level

NPC Inverter can be operated in 3-Phase 4-Wire Case. So, the Tri-level NPC Inverter can be considered as a flexible circuit configuration for 3Phase 3-Wire and/or 4Wire System.

The control strategy can be performed by 3dimensional techniques in $\alpha \beta 0$ frame, such as the 3D Cubical Hysteresis, Cylindrical Coordinate Controls and 3D Space Vector Modulation [7][8][9]. Equation (1) expresses the transformation from abc into $\alpha \beta 0$ frame. Conventionally, the zero-frame is not included in the transformation. However, zero-frame is needed for neutral wire voltage or current control in 3-phase 4 -wire system.

$$
\left[\begin{array}{l}
v_{\alpha}  \tag{1}\\
v_{\beta} \\
v_{0}
\end{array}\right]=\sqrt{\frac{2}{3}}\left[\begin{array}{ccc}
1 & -1 / 2 & -1 / 2 \\
0 & \sqrt{3} / 2 & -\sqrt{3} / 2 \\
1 / \sqrt{2} & 1 / \sqrt{2} & 1 / \sqrt{2}
\end{array}\right]\left[\begin{array}{l}
v_{a} \\
v_{b} \\
v_{c}
\end{array}\right]
$$

Based on (1), switching function and consideration of equivalent circuit of Tri-level NPC Inverter, shown in Fig. 5 , the mathematical model of 3D voltage space vector can be constructed as (2). Switching function can be $S_{j} \in\{-1$, $0,1\}$ in 3-level, where j can be $\mathrm{a}, \mathrm{b}$ or c . $\mathrm{V}_{\mathrm{dc}}$ is assumed to be $\mathrm{V}_{\mathrm{dc}}=\mathrm{V}_{\mathrm{dc} 1}=\mathrm{V}_{\mathrm{dc} 2}$.


Fig. 5 Equivalent Circuit of Tri-Level NPC 3-Phase 4-Wire Inverter $\stackrel{\rightharpoonup}{v}=V_{d c}\left[\sqrt{\frac{2}{3}} S_{\alpha} \cdot \vec{n}_{\alpha}+\frac{1}{\sqrt{2}} S_{\beta} \cdot \vec{n}_{\beta}+\frac{1}{\sqrt{3}} S_{0} \cdot \vec{n}_{0}\right]$
, where

$$
\begin{gather*}
S_{\alpha}=S_{a}-\frac{1}{2} S_{b}-\frac{1}{2} S_{c}  \tag{2}\\
S_{\beta}=S_{b}-S_{c} \\
S_{0}=S_{a}+S_{b}+S_{c}
\end{gather*}
$$

According to the above consideration, the 3 dimensional voltage space vectors can be described as shown in Fig. 6.


According to the d.c. voltage variation that based on the analysis of the switching state and equivalent circuit, those vectors can be classified as Larger-Than-Zero-Axis, Equal-To-Zero-Axis and Smaller-Than-Zero-Axis Vectors. In Table 2, the characteristics of Tri-Level NPC 3-Phase 4-Wire Inverter is summarized.

Table 2
SUMMARY OF 3-LEVEL NPC 3-PHASE 4-WIRE INVERTER

| Vector Number | Voltage Space Vector | Switching Patterns | Group | Available State | DC <br> Voltage Variation |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | $\bar{V}_{000}$ | \{0,0,0\} | Equal-to- Zero | 1 | unknown |
| 2 | $\bar{V}_{\text {oup }}$ | \{1,1,1\} | $\begin{array}{\|l\|} \hline \text { Larger- } \\ \text { Than-Zero } \\ \hline \end{array}$ | 2 | Upper Decrease |
| 3 | $\bar{V}_{\text {oon }}$ | $\{-1,-1,-1\}$ | $\begin{aligned} & \hline \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 3 | Lower Decrease |
| 4 | $\vec{V}_{1}$ | \{1,-1,-1\} | $\begin{aligned} & \hline \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 4 | Lower Decrease |
| 5 | $\vec{V}_{2}$ | \{1,1,-1\} | $\begin{aligned} & \hline \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 5 | Upper Decrease |
| 6 | $\vec{V}_{3}$ | $\{-1,1,-1\}$ | $\begin{array}{\|l\|} \hline \text { Smaller- } \\ \text { Than-Zero } \\ \hline \end{array}$ | 6 | Lower Decrease |
| 7 | $\vec{V}_{4}$ | $\{-1,1,1\}$ | $\begin{aligned} & \hline \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 7 | Upper Decrease |
| 8 | $\overline{\bar{V}_{5}}$ | $\{-1,-1,1\}$ | $\begin{aligned} & \hline \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 8 | Lower Decrease |
| 9 | $\bar{V}_{6}$ | \{1,-1,1\} | Larger-Than-Zero | 9 | Upper Decrease |
| 10 | $\vec{V}_{12}$ | \{1,0,-1\} | $\begin{aligned} & \hline \text { Equal-to- } \\ & \text { Zero } \\ & \hline \end{aligned}$ | 10 | unknown |
| 11 | $\vec{V}_{23}$ | \{0,1,-1\} | $\begin{aligned} & \text { Equal-to- } \\ & \text { Zero } \\ & \hline \end{aligned}$ | 11 | unknown |
| 12 | $\vec{V}_{34}$ | $\{-1,1,0\}$ | $\begin{aligned} & \text { Equal-to- } \\ & \text { Zero } \end{aligned}$ | 12 | unknown |
| 13 | $\bar{V}_{45}$ | $\{-1,0,1\}$ | $\begin{aligned} & \text { Equal-to- } \\ & \text { Zero } \end{aligned}$ | 13 | unknown |
| 14 | $\vec{V}_{56}$ | \{0,-1, 1 \} | $\begin{aligned} & \text { Equal-to- } \\ & \text { Zero } \\ & \hline \end{aligned}$ | 14 | unknown |
| 15 | $\bar{V}_{61}$ | \{1,-1,0\} | $\begin{array}{\|l} \hline \text { Equal-to- } \\ \text { Zero } \\ \hline \end{array}$ | 15 | unknown |
| 16 | $\bar{V}_{01 p}$ | \{1,0,0\} | $\begin{array}{\|l\|} \hline \text { Larger- } \\ \text { Than-Zero } \\ \hline \end{array}$ | 16 | $\begin{aligned} & \hline \text { Upper } \\ & \text { Decrease } \end{aligned}$ |
| 17 | $\vec{V}_{0 n}$ | $\{0,-1,-1\}$ | $\begin{aligned} & \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 17 | $\begin{aligned} & \text { Lower } \\ & \text { Decrease } \end{aligned}$ |
| 18 | $\vec{V}_{02 p}$ | \{1,1,0\} | $\begin{aligned} & \hline \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 18 | Upper Decrease |
| 19 | $\vec{V}_{02 n}$ | \{0,0,-1\} | $\begin{aligned} & \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 19 | Lower Decrease |
| 20 | $\vec{V}_{03 p}$ | \{0,1,0\} | $\begin{aligned} & \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 20 | Upper Decrease |
| 21 | $\vec{V}_{03}$ | \{-1,0,-1\} | $\begin{aligned} & \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 21 | $\begin{aligned} & \hline \text { Lower } \\ & \text { Decrease } \\ & \hline \end{aligned}$ |
| 22 | $\vec{V}_{04 p}$ | \{0,1,1\} | $\begin{aligned} & \hline \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 22 | Upper Decrease |
| 23 | $\vec{V}_{04,}$ | \{-1,0,0\} | Smaller- <br> Than-Zero | 23 | Lower Decrease |
| 24 | $\vec{V}_{05 p}$ | \{0,0,1\} | $\begin{aligned} & \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 24 | Upper Decrease |
| 25 | $\vec{V}_{05 n}$ | $\{-1,-1,0\}$ | $\begin{aligned} & \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 25 | Lower Decrease |
| 26 | $\vec{V}_{06 p}$ | \{1,0,1\} | $\begin{aligned} & \text { Larger- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 26 | Upper Decrease |
| 27 | $\vec{V}_{06 n}$ | $\{0,-1,0\}$ | $\begin{aligned} & \text { Smaller- } \\ & \text { Than-Zero } \\ & \hline \end{aligned}$ | 27 | $\begin{aligned} & \hline \text { Lower } \\ & \text { Decrease } \\ & \hline \end{aligned}$ |

Fig. 6 3D Voltage Space Vector's Allocation

In Tri-level NPC 3-Phase 4-Wire Inverter, the number of switching states is equal to the number of the available vectors. There are Larger-Than-ZeroAxis $\left\{\vec{V}_{00 p}, \vec{V}_{2}, \vec{V}_{4}, \vec{V}_{6}, \vec{V}_{0 \psi}, \vec{V}_{02 p}, \vec{V}_{03 p}, \vec{V}_{04 p}, \vec{V}_{05 p}, \vec{V}_{06 p}\right\}$, Equal-To-Zero-Axis $\left\{\vec{V}_{000}, \vec{V}_{12}, \dot{\vec{V}}_{23}, \vec{V}_{34}, \vec{V}_{45}, \vec{V}_{56}, \vec{V}_{61}\right\}$ and Smaller-Than-Zero-Axis $\left\{\vec{V}_{00 n}, \vec{V}_{1}, \vec{V}_{3}, \vec{V}_{5}, \vec{V}_{01 n}, \vec{V}_{02 n}, \vec{V}_{03 n}\right.$, $\vec{V}_{04 n}, \vec{V}_{05 n}, \vec{V}_{06 n}$ \}vectors. When one of the Larger-Than-Zero-Axis vectors $\left\{\vec{V}_{00 \rho}, \vec{V}_{2}, \vec{V}_{4}, \vec{V}_{6}, \vec{V}_{01 p}, \vec{V}_{02 p}, \vec{V}_{03 p}\right.$, $\left.\vec{V}_{04 p}, \vec{V}_{05 p}, \vec{V}_{06 p}\right\}$ is chosen, $v_{d c 1}<v_{d c 2}$ will occur and vice versa. However, if the one of the Equal-To-Zero Vectors is activated, the d.c. voltage variation cannot be known.

## C. Similarities and Differences of Tri-level NPC 3Phase 3-Wire and 3-Phase 4-Wire Inverters

Tri-level NPC Inverter can operate as 3-Phase 3-Wire or 3-Phase 4Wire Operation; it depends on whether the neutral wire is connected with the mid-point of the capacitors, shown in Fig. 3.

There are 27 switching vectors in a Tri-level inverter; however, there are only 19 available states in 3-Phase 3Wire case. On the other hand, there are 27 switching states in 3-Phase 4Wire one. Furthermore, the control strategies should be extended from 2-dimensional situation ( $\alpha \beta$ frame) into 3 -dimensional space ( $\alpha \beta 0$ frame). Besides, the different switching state may activate different d.c. voltage variation, such as summarized in Table 1 and Table 2.

In Tri-level NPC 3-Phase 3-Wire Inverter, only vectors $\left\{\bar{V}_{000}, \vec{V}_{00 \rho}, \vec{V}_{000}, \vec{V}_{1}, \vec{V}_{2}, \vec{V}_{3}, \vec{V}_{4}, \vec{V}_{5}, \vec{V}_{6}\right\}$ cannot take any influence on the d.c. voltage variation. If only the above vectors are activated in all control periods, there is no need to consider the d.c. voltage variation in Tri-level NPC 3-Phase 3-Wire Inverter. On the other hand, there is no the case in Tri-level NPC 3-Phase 4-Wire Inverter, all the switching vectors will affect the d.c. voltage variation.

In order to control the tendency of d.c. voltage variation, the p-type or n-type vectors can be chosen. The p-type vectors can be defined as $\vec{V}_{01 p}, \vec{V}_{02 p}, \vec{V}_{03 p}$, $\bar{V}_{04 p}, \bar{V}_{05 p}, \bar{V}_{06 p}$. Besides, the n-type vectors $\operatorname{are} \vec{V}_{01 n}, \vec{V}_{02 n}, \vec{V}_{03 n}, \vec{V}_{04 n}, \vec{V}_{05 n}, \vec{V}_{06 n}$. When the p-type vector is activated, the voltage of the upper arm d.c. capacitor will trend to be decreased, and vice versa. No matter it is 3 phase 3-wire or 3 phase 4 wire Tri-level NPC Inverter, the activation of p-type vector will decrease the voltage of the upper arm d.c. capacitor, and the activation of n-type vector will increase the voltage of the upper arm d.c. capacitor. However, the $\vec{V}_{12}, \vec{V}_{23}, \vec{V}_{34}, \vec{V}_{45}, \vec{V}_{56}$ and $\vec{V}_{61}$ vectors cannot be employed to control the tendency of d.c. voltage variation in 3-phase 3 wire or 3 -phase 4 wire system.
D. d.c. Voltage Variation

If the d.c. side voltage turns to be unbalance, there are 2 cases needed to be considered: the waveform quality of the inverter's output and the safety operation of the inverter. For the first issue, the waveform quality can be improved by following approach for 3-phase 4-wire system. When $v_{d c 1} \neq v_{d c 2}$, the $V_{d c}$ can be redefined as (3) so that the new switching function can be expressed as (4) for upper and lower arms respectively.

$$
\begin{gather*}
V_{d c}=\frac{v_{d c 1}+v_{d c 2}}{2}  \tag{3}\\
S_{j}^{N}=\left\{\begin{array}{lll}
v_{d c 1} / V_{d c}, & \text { upper } & \text { arm } \\
-v_{d c 2} / V_{d c}, & \text { lower } & \text { arm }
\end{array}\right. \tag{4}
\end{gather*}
$$

Substitute (3) into (4), equation (5) can be obtained. It is obvious that when the d.c. voltage is changed, the value of switching function can be changed too. The switching function can be larger than or less than 1 when the d.c. voltage is varied.

$$
\begin{align*}
S_{j}^{N}= & \begin{cases}1+\Delta S, & \text { upper arm } \\
-1+\Delta S, & \text { lower arm }\end{cases}  \tag{5}\\
& \Delta S=\frac{v_{d c 1}-v_{d c} 2}{2 V_{d c}} \text { and } \mathrm{j}=\mathrm{a}, \mathrm{~b} \text { or } \mathrm{c} .
\end{align*}
$$

, where
Equation (5) is in abc frame and can transferred into $\alpha \beta 0$ frame by (1) so that (6), (7) and (8) can be received.

$$
\begin{align*}
& S_{\alpha}^{N}=S_{\alpha}  \tag{6}\\
& S_{\beta}^{N}=S_{\beta}  \tag{7}\\
& S_{0}^{N}=S_{0}+3 \Delta S \tag{8}
\end{align*}
$$

From the above equations, it can be concluded that the d.c. voltage variation will only influence the zero switching function. Substitute (5) into (2), equation (9) can be received.

$$
\begin{equation*}
\vec{v}^{N}=\vec{v}+\vec{v}_{0}^{N} \tag{9}
\end{equation*}
$$

where $\vec{\nu}_{0}^{N}=\sqrt{3} V_{d c} \Delta S \cdot \vec{n}_{0}$.
According to the above discussion, if the d.c. side voltage is changed, voltage vector reference should be altered accordingly in order to reduce the affect of the voltage variation so as to improve the output waveform quality. In Tri-level NPC 3phase 4 wire system, the zero frame is included in the calculation by 3D techniques. However, in Tri-level 3-phase 3-wire system, zero-frame is not included in the PWM calculation so that p-type and n-type vectors should be chosen in order to reduce the d.c. voltage variation so as to improve the waveform quality.

For the second issue, the safety operation of inverter should be considered due to the d.c. voltage unbalance. If voltage of one arm of the d.c. side capacitor is too large, the IGBTs or the capacitors may reach the maximum limit of rated voltage so as to destroy the components of inverter. The vectors in Table 1 and Table 2 should be chosen accordingly for 3-phase 3 -wire and 3 -phase 4 wire systems respectively in order to
control the d.c. voltage variation. In 3-Phase 4Wire Inverter, the Larger-Than-Zero-Axis vectors should be chosen in order to control the tendency of upper-arm d.c. voltage variation to be decreasing.

## IV. Simulation Results

The control strategy of 3DSVM for 3-arm center-split inverter is out of the discussion in this paper. And there are numerous simulated and experimental results had been performed for Tri-Level NPC 3-Phase 3-Wire Inverter so that there is no result about it in the following sections. The simulated results show that the output waveform quality can be improved by the above proposed strategy in Section III. D.


Fig. 7 Compensation Result without the Consideration of d.c. Voltage Variation


Fig. 8 Compensation Result with the Consideration of d.c. Voltage Variation
Fig. 7 shows that the $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and neutral wire currents after compensation when the d.c. voltage variation is out of consideration into the vector reference. In the Fig. 7 and Fig. 8, the upper-arm d.c. voltage is reduced into 30 $\%$ of its original value, besides the lower-arm d.c. voltage of inverter is increased up to $70 \%$ of its normal value respectively. Fig. 8 shows that the output waveform quality can be improved if the vector reference in zeroaxis is altered according to the d.c. voltage variation.

## V. EXPERIMENTAL RESULTS

A Tri-level NPC 3-phase 4-wire inverter prototype is implemented. The control strategy is performed by 3DSVM with 5 KHz switching frequency. The DSP Controller is chosen as TMS320F2407. The value of d.c. side capacitor is 10 mF . The system configuration is as shown in Fig. 9.

The experimental results show that the Tri-level NPC Inverter can be operated as the 3 phase 4 wire power quality compensator to reduce the harmonics, unbalance and neutral currents.


Fig. 10 Current Waveforms before Compensation


Fig. 11 Current Waveforms after Compensation


Fig. 12 d.c. Voltage Variation without Control


Fig. 13 d.c. Volage Variation with Control
Fig. 10 and Fig. 11 show the $\mathrm{a}, \mathrm{b}, \mathrm{c}$ and neutral wire currents before compensation and after compensation respectively. Fig. 12 shows the d.c. side capacitor voltage variation without control. However, when the Larger-Than-Zero-Axis or Smaller-Than-Zero-Axis vectors are chosen for compensation according to the change of d.c. voltage, the d.c. capacitor voltage variation can be controlled as the experimental result shown in Fig. 13.

## VI. CONCLUSION

In this paper, the theoretical difference and similarity of Tri-Level NPC Inverters operating in 3-Phase 3-Wire and 3 -phase 4 -Wire systems are discussed. It shows that the same circuit configuration of Tri-Level NPC Inverter can be employed for 3-Phase 3-Wire and 3-phase 4-Wire systems. With only a wire to be connected between the mid-point of capacitors of Tri-level NPC Inverter and neutral wire of system, the inverter can turn into 3-phase 4 -wire operation.

In Tri-level NPC 3Phase 3-Wire Inverter, some of the vectors, $\left\{\vec{V}_{000}, \vec{V}_{00 p}, \vec{V}_{00 n}, \vec{V}_{1}, \vec{V}_{2}, \vec{V}_{3}, \vec{V}_{4}, \vec{V}_{5}, \vec{V}_{6}\right\}$, cannot take any influence on the d.c. voltage variation. On the other hand, there is no such case in Tri-level NPC 3-Phase 4 Wire Inverter, all the switching vectors will affect the d.c. voltage variation.

In order to control the tendency of d.c. voltage variation, the p-type, $\left\{\vec{V}_{01 p}, \vec{V}_{02 p}, \vec{V}_{03 p}, \vec{V}_{04 p}, \vec{V}_{05 p}, \vec{V}_{06 p}\right\}$, or ntype, $\left\{\vec{V}_{01 n}, \vec{V}_{02 n}, \vec{V}_{03 n}, \vec{V}_{04 n}, \vec{V}_{05 n}, \vec{V}_{06 n}\right\}$, vectors can be chosen. When the p-type vector is activated, the voltage of the upper arm d.c. capacitor will trend to be decreased, and vice versa. No matter it is 3 -phase 3 -wire or 3 -phase 4 wire Tri-level NPC Inverter, the activation of p-type vectors will decrease the voltage of the upper arm d.c. capacitor, and the activation of n-type vectors will increase the voltage of the upper arm d.c. capacitor. However, the $\vec{V}_{12}, \vec{V}_{23}, \vec{V}_{34}, \vec{V}_{45}, \vec{V}_{56}$ and $\vec{V}_{61}$ vectors cannot be employed to control the tendency of d.c. voltage variation in 3 -phase 3 -wire or 3 -phase 4 -wire Tri-level NPC Inverter. In 3-Phase 4Wire Tri-Level NPC Inverter, the Larger-Than-Zero-Axis Vectors or Smaller-Than-Zero-

Axis Vectors can be chosen to control the tendency of d.c. voltage variation accordingly. The output waveform quality can be improved by consideration of zero-axis of the vector reference in the control strategy due to the d.c. voltage variation for 3-Phase 4-Wire System.

## ACKNOWLEDGMENT

The authors would like to thank you for the financial supports of Research Committee of University of Macau and Tsinghua University.

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