Human activity recognition by manifold regularization based dynamic graph convolutional networks

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Abstract

Deep learning has shown superiority to extract more representative features from multimedia data in recent years. Recently, the most typical graph convolutional networks (GCN) has achieved excellent performance in the semi-supervised framework-based data representation learning tasks. GCN successfully generalizes traditional convolutional neural networks to encode arbitrary graphs by exploiting the graph Laplacian-based sample structure information. However, GCN only fuses the static structure information. It is difficult to guarantee that its structure information is optimal during the training process and applicable for all practical applications. To tackle the above problem, in this paper, we propose a manifold regularized dynamic graph convolutional network (MRDGCN). The proposed MRDGCN automatically updates the structure information by manifold regularization until model fitting. In particular, we build an optimization convolution layer formulation to acquire the optimal structure information. Thus, MRDGCN can automatically learn high-level sample features to improve the performance of data representation learning. To demonstrate the effectiveness of our proposed model, we apply MRDGCN on the semi-supervised classification tasks. The extensive experiment results on human activity datasets and citation network datasets validate the performance of MRDGCN compared with GCN and other semi-supervised learning methods.

1. Introduction

With the advancement of science and technology, and the popularity of smart terminals such as smartphones and notebook computers, large scale multimedia data (e.g. document, picture, audio and video) are generated and uploaded to the Internet every day. Image is one of the largest, fastest growth speed and most informative multimedia data carriers in the current society. Therefore, images classification and recognition, such as human activity recognition (HAR) [1–3], face recognition [4–6], pedestrian detection [7–9] and object detection [10–12], have become an important part of computer vision, pattern recognition and machine learning in recent years, which can effectively analyze the content of digital images and give correct judgments. With the development of virtual reality and augmented reality, HAR has attracted much attention in many areas including video surveillance and accident warning. However, traditional conventional shallow learning algorithms including support vector machine [13], kernel least squares [14] and logistic regression [15] cannot extract more representative sample features and meet development needs, which directly affect the results of the image classification tasks.

To acquire high-level sample features from massive images, deep learning (DL) was introduced and has been demonstrated to be an effective method. In practical life, a small amount of labeled samples are readily available, whereas massive labeled samples cannot be directly obtained because it require a lot of manpower, material resources and financial resources. The most successful method is semi-supervised learning with manifold regularization (MRSSL), which uses the manifold structure information of unlabeled and labeled samples distribution by regarding it as a regularization term of the objective function. That is to say, any two samples with the closer space distance generally belong to the same category. Liu et al. [16] presented a kernel logistic regression with Laplacian regularization for web image annotation by employing the graph Laplacian to preserve the local geometry of the potential manifold. Tao et al. [17] proposed a Hessian regularized support vector machines model to improve the performance.
of image annotation due to the richer null space of Hessian. Liu et al. [18] combined p-Laplacian with support vector machines and kernel least squares by utilizing p-Laplacian to express high-order manifold distribution. Ma et al. [19] utilized hypergraph p-Laplacian to capture the complex relationships among the different samples.

MRSSL methods are only effective for regular Euclidean data. There exists vast amounts of non-Euclidean data or graph data of arbitrary structures. In recent years, spectral convolution methods have received an increasing attention and achieved better performance including text classification [20–22] and image recognition [23–25]. Each node of graphs gathers its neighbors information by the convolution operation of the Fourier domain, in other words, this method does not directly make the convolution on the graphs. Kipf and Welling [26] presented a graph convolutional networks to learn the sample features by fusing the direct neighbors relationships of each node. Fu et al. [27] considered the direct and indirect neighbors relationships to learn richer sample features, which improved the performance of semi-supervised classification. Yadati et al. [28] proposed a hypergraph-based GCN for document classification by using hypergraph to describe the multicultural relationships among samples.

However, the above methods depend on the static samples distribution, which limit the range of its application. Confronting this challenging problem, it is important to design a dynamic graph structure learning model, which aims to automatically optimize the local geometry of samples. In this paper, we propose a dynamic graph convolutional network based on manifold regularization (MRDGCN) for semi-supervised classification. We introduce a manifold regularization term to the objective function, which can drive the objective function to change over the potential sample distribution manifold. When the objective function value cannot meet a specific threshold, MRGCN separately updates or optimizes its manifold structure information (except the first convolution layer) and network weight matrix until model fitting. After many times training iteration, our proposed MRGCN can acquire optimal structure information. In addition, we make an optimization and derivation for the convolution layer formulation of GCN, and then propose a general graph structure learning framework. Finally, MRDGCN can extract more high-level sample features by fusing its dynamic structure information to improve the performance of the semi-supervised classification. To verify the performance of our proposed MRDGCN model, we have tested on CAS-YNU-IN datasets for citation networks classification. To further build a linear and deep model, Kipf and Welling limited the order of the Chebyshev polynomials (K = 1), in other words, it only considered the direct relationships between any two samples. Finally, it acquired a linear convolution layer formulation, i.e. \( H^{k+1} = \sigma(BH^kW^k) \). \( B \) is equal to \( D^{-\frac{1}{2}}(A + I)D^{-\frac{1}{2}} \). \( W^k \) is weight parameter matrix to be learned in the training iteration process. The detailed evolution process can be found in [26]. During the training process of GCN, it increased the number of training iteration according to value of cross entropy loss objective function and will stop until model fitting.

3. Manifold regularized dynamic graph convolutional networks

MRDGCN can learn more effective sample features by continuously updating manifold distribution information of samples apart from the first convolution layer during the convolution process, which yields better classification performance than GCN model. We first introduce the traditional manifold regularized framework to original objective function of GCN, and then propose a dynamic graph structure learning (DGSL) method. Following, we give the optimization scheme of DGSL on each training iteration. To solve the application limitation of GCN on different datasets, in the last, we present the derivation and optimization scheme of each convolution layer formulation for DGSL. And then we analyze the implement process of a two-layer MRDGCN. Fig. 1 shows the general framework of our proposed MRDGCN.

3.1. Dynamic graph structure learning

GCN relies on a static sample manifold distribution information \( B \) that is computed according to the input data. That is to say, this method only optimized weight matrix \( W^k \) of each convolution layer. In real life, the local geometry distribution between data always in changing, thus GCN cannot get the most effective sample features. To tackle this issue, we apply traditional manifold regularization framework to the cross entropy loss function of GCN, and then propose a DGSL model to encode the complex data structure. In other words, we update the structure relationships (apart from the first convolution layer) and weight parameters simultaneously by adding an additional manifold regularization term to the cross entropy loss function. Therefore, our proposed DGSL can be denoted as the following optimization issue, i.e.

\[
C(W, A) = C_1(W, A) + \beta C_2(W, A) = -y \log Y + \beta \text{tr} \left( Y^tMY \right)
\]
In DGSL, $C_1(W, A)$ denotes the cross entropy loss. $\text{tr}(Y^T MY)$ represents the manifold regularization term. $M$ denotes that how to use more effective method including graph Laplacian, Hessian and $p$-Laplacian, to better preserve the local geometric distribution of samples. In this paper, we use universally used graph Laplacian matrix. $y$ is the label information matrix of the input sample. $Y$ denotes the probability distribution matrix of samples, i.e. we can get $Y$ by taking the extracted sample features $H^{(k+1)}$ of the last convolution layer as the input of the Softmax function. Thus, the above objective function can be written as:

$$C(W, A) = -y \log Y + \beta \text{tr}(Y^T LY)$$

We can regard the objective function of DGSL as a dual optimization issue, i.e. we need to update or optimize two variable $W$ and $A$. $\beta$ is a balance parameter of the objective function.

### 3.2. Optimization scheme

In this paper, we use the alternative optimization strategy to update adjacency matrix and weight matrix, i.e. when we update a specific variable, we fix others variable until the objective function of DGSL meet a specific threshold or remain unchanged for many times. We first fix the adjacency matrix $A$ and optimize weight matrix $W$, thus the above objective function can be simplified as the following form:

$$C(W) = -y \log Y + \beta \text{tr}(Y^T LY)$$

(5)

where the initial $A$ of each convolution layer is calculated according the input samples by k-NearestNeighbor with the Euclidean distance. In this paper, this problem can be solved by the gradient descent method [29].

Following, we fix weight matrix $W$, the above objective function on updating adjacency matrix $A$ (except for the first convolution layer) can be denoted as

$$C(A) = -y \log Y + \beta \text{tr}(Y^T LY)$$

(6)

The $A$ can be updated according to output sample features of final convolution layer of the last training iteration. With the update of adjacency matrix $A$, we also further make an optimization for the weight matrix $W$. Our proposed DGSL will repeat this process until the objective function value do not come down for many epochs.

#### 3.3. A two-layer MRDGCN

To increase the scale adaptability of model, GCN let $\lambda_{\max} = 2$. With the diversification of adjacency matrix $A$ computing methods and the differences between different datasets, $\lambda_{\max} = 2$ has the limitation. To solve this problem, we make an optimization for the one-order spectral graph convolution again, and then the spectral convolution with one-order polynomial can be simplified as the following form:

$$g_{\theta_3}(X)\star X = \sum_{k=0}^{k=1} \theta_3 T_k\left(L\right) X = \theta_3 X + \theta_1 \left(\frac{2}{\lambda_{\max}}L - I_N\right) X$$

(7)

where $\theta_0$ and $\theta_1$ denote the filter parameters, i.e. weight matrix $W^{(1)}$ of each convolution layer. To further avoid the overfitting issue of the above formula, we can get the following expression by using a single parameter $\theta$, i.e.

$$g_{\theta_3}(X)\star X = \left(\theta_0 - \theta_1 + \frac{2}{\lambda_{\max}} \theta_1 \left(I_N - D^{-\frac{1}{2}}AD^{-\frac{1}{2}}\right)\right) X$$

$$= \left(\theta_2 + \frac{2}{\lambda_{\max}} \theta_1 \left(I_N - D^{-\frac{1}{2}}AD^{-\frac{1}{2}}\right)\right) X$$

$$= \left(\frac{2}{\lambda_{\max}} \theta_2 + \theta_1 \right) X - \frac{2}{\lambda_{\max}} \theta_1 D^{-\frac{1}{2}}AD^{-\frac{1}{2}} X$$

$$= \left(\frac{2}{\lambda_{\max}} \theta_2 + \theta_1 \right) X - \frac{2}{\lambda_{\max}} \theta_1 D^{-\frac{1}{2}}AD^{-\frac{1}{2}} X$$

(8)

where, $\theta_0 - \theta_1 = \theta_2$, $\theta_0 + \theta_1 = \theta_3$ and $\theta_2 - \theta_1 = \theta$. To further avoid vanishing gradients and instabilities by stacking the above form to build a deep network model, we also introduce the renormalization trick that is suggested in [26]. And then we get an optimization convolution layer formulation for a signal $X \in R^{n \times m}$ with $n$
samples and $m$ dimensional sample features, which is named the manifold regularized dynamic graph convolutional networks (MRDGCN), i.e.
\[
g_x(l) = \frac{2}{\lambda_{\max}} \tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}} X \theta = \frac{2}{\lambda_{\max}} B^{(l)} H^{(l)} W^{(l)}
\]
(9)
where $\theta \in \mathbb{R}^{n \times z}$ or $W^{(l)}$ is filter parameter of each network layer.
\[ A = \tilde{A} + I_h \text{ and } B^{(l)} = \tilde{D}^{-\frac{1}{2}} \tilde{A} \tilde{D}^{-\frac{1}{2}}. \]
The dynamic spectral convolution can be interpreted as the following process: (1) During the first iteration training process, when the loss values of the objective function Eq. (4) meet a specific threshold, MRDGCN will stop training. Otherwise, MRDGCN will constantly optimize the adjacency matrix and weight matrix of each layer by the alternative optimization strategy, and then will implement the second iteration training. (2) MRDGCN will repeat the above process until the objective function Eq. (4) meets a specific threshold. (3) Finally, MRDGCN can acquire the optimal adjacency matrix and weight matrix. After multi-layer spectral convolutions, it can learn richer data information to improve the classification performance.

**Algorithm 1:** A two-layer manifold regularized dynamic graph convolutional networks

| Input: Datasets $X$ |
| Parameter: $\beta$, training iteration epoch $k$, learning rate etc. |
| Output: Recognition accuracy |

1: $H^{(1)} = \text{RELU} \left( \frac{2}{\lambda_{\max}} B^{(0)} X W^{(0)} \right)$. 
2: $H^{(2)} = \frac{2}{\lambda_{\max}} B^{(1)} H^{(1)} W^{(1)}$. 
3: for $j = 0 \rightarrow k - 1$
4: Fix $A$, optimize $W$ by Eq. (5). 
5: Fix $W$, update $A$ by Eq. (6).
6: end for
7: Get the optimal $A, W$ and $H^{(2)}$.
8: Give the recognition accuracy.

In this paper, we use a two-layer MRDGCN for semi-supervised classification to demonstrate the effectiveness of our proposed method. And then, we can get the following formulation by stacking two-layer Eq. (9), i.e.
\[
H^{(2)} = \frac{2}{\lambda_{\max}} B^{(1)} \text{RELU} \left( \frac{2}{\lambda_{\max}} B^{(0)} X W^{(0)} \right) W^{(1)}
\]
(10)
where $X$ denotes the initial sample features. After two-layer convolution operation, MRDGCN can efficiently learn the sample features with $n$ samples and $Q$ dimensional (The number of $Q$ is equal to classes). Following, we can get the probability distribution matrix $Y$, and then can get the optimal structure information of the second layer and weight matrix by our proposed optimization scheme after many training iteration. Finally, MRDGCN can extract more representative sample features by fusing the optimal structure information and give the recognition accuracy by Softmax classifier. Algorithm 1 summarize a two-layer manifold regularized dynamic graph convolutional networks.

4. Experiments

To demonstrate the effectiveness of our proposed algorithm, in this section, we conduct substantial experiments to test the proposed MRDGCN, MRDGCN-1 and other semi-supervised learning methods, such as the representative GCN [26], graph attention networks (GAT) [30], Hypergraph $\ell$-Laplacian graph convolutional networks (HpLapGCN) [31], Chebyshev ($K = 3$) [20], Chebyshev ($K = 3$) [20], HyperGCN [28], manifold regularization (ManiReg) [32], semi-supervised embedding (SemiEmb) [33], multi-layer perceptron (MLP) [26], skip-gram based graph embeddings (DeepWalk) [34], on several human activity datasets and citation network datasets. The baseline MRDGCN-1 denotes the combination of optimized GCN variation Eq. (9) and cross entropy loss function [26], which still use a static sample structure information. MRDGCN is constructed by the optimized convolution layer formulation Eq. (9) and our proposed objective function Eq. (4). Following, we detailed present the used datasets, experiment parameters setting and comparison results, respectively.

4.1. Experiment datasets

CAS-YNU-MHAD dataset [2], a multimodal human activity database, was created by the Chinese Academy of Sciences and Yunnan University. It was collected by utilizing a Microsoft Kinect camera and 17 inertial sensors, which were placed in spine, left shoulder, right shoulder, left arm, right arm, left forearm, right forearm, left hand, right hand, spine, hips, right up leg, left up leg, left leg, right leg, left foot and right foot. It is composed of 1086 human actions with 10 different classes, such as typing, lying down, walking 5, walking quickly, walking, sitting up, sitting down, running, jumping up and jumping forward. Each category was collected from 10 people between 20 and 30 years old. The original depth human action image is resized to 512 × 424 pixels with 16-bit. We also use the same feature extraction method that is suggested in [22] to acquire the STCP features [35] of each depth human action image, i.e. we can get a feature matrix with 1086 samples and 81648 dimensions.

Unstructured social activity attribute (USAA) dataset [1,36] is composed of totally 1600 videos collected from the Columbia Consumer Video (CCV) [37] database. USAA consists of eight semantic category videos collected from birthday party, music performance, non-music performance, parade, wedding dance, wedding ceremony, graduation party and wedding reception. USAA provides the static SIFT features and spatial–temporal interest points (STIP) features. In our experiments, we use the video features that concatenate SIFT and STIP to learn more effective sample features via MRDGCN, i.e. each video has 10000 dimensional features.

The 2moons database is a virtual human action database constructed by humans, which contains 200 images. All images are selected into 2 categories, which is distinguished by label +1 (moon images) or labeled −1 (non-moon images).

Citeseer dataset [38] consists of 3327 machine learning publications with 3703 dimensional features, which is collected from six classes including Agents, AI, IR, HCI, DB and ML.

Cora dataset [39] is composed of 2708 publications with 1433 dimensional features, which are totally seven categories, such as reinforcement-learning, case-based, probabilistic-methods, neural-networks, theory, genetic-algorithms and rule learning.

4.2. Experiment parameters

In our semi-supervised classification experiments, for CAS-YNU-MHAD dataset, 200 samples are randomly selected as test set, 200 samples are randomly choose as validation set, and the remaining part for training set. For USAA database, we use 300 samples for validation set, 300 samples for testing and the rest videos for training. To demonstrate the classification performance of our proposed method under few labeled training data, in its training set (CAS-YNU-MHAD and USAA), we randomly chose $10\%$, $20\%$, $30\%$, $40\%$ and $50\%$ samples as labeled data and the rest samples for unlabeled data. Because the 2moons dataset is quite small, we randomly select 50 samples as validation samples, 50 samples for test examples and the rest as training samples. In addi-
tion, we randomly assign a specific label rate including 5%, 10%, 15%, 20% and 25% as labeled samples and the rest part as unlabeled samples on the 2moons database. For Citeseer and Cora dataset, we choose 1000 samples as test samples, 500 samples as validation samples and the rest as training samples.

To minimize the loss value of our proposed objective function, the Adam optimizer [40] with an initialized learning rate of 0.01 and 0.001 (USAA) is used to train a two-layer MRDGCN. The maximum training iteration up to 200 epochs and MRDGCN will early stopping training if the loss value of objective function do not descend for 10 times continuously on its validation set. We use the weights initialization method that is suggested in [41] during the training process. The L2 regularization with a regularization parameter of $5 \times 10^{-4}, 5 \times 10^{-5}$ (USAA) and the dropout [42] with a dropout rate of 0.5 is used to solve the overfitting problem of MRDGCN. The balance parameter $\beta$ of objective function is 0.001 and 1 (USAA). In addition, on the CAS-YNU-MHAD, USAA, 2moons datasets and citation network datasets, the output feature dimension of the first convolution layer is 128, 32, 16 and 16, respectively.

4.3. Citation networks classification – toy experiment

In the GCN and most of existing GCN variant models, the commonly-used datasets are citation networks datasets. Thus, we also make a comparison on the Citeseer and Cora datasets for our proposed MRDGCN. We use 120 and 140 labeled samples on the Citeseer and Cora training samples respectively and give the mean recognition rate with 100 random runs. As shown in Table 1, we can find that our proposed MRDGCN model performs better than the state-of-the-art methods, which also indicates that MRDGCN can better preserve and utilize the structure relationships of the samples via manifold regularization method. It also reveals that MRDGCN can learn more representative sample features by dynamically updating the manifold distribution of the samples during the training process.

4.4. Human activity recognition

Figs. 2–4 show the histogram of the recognition rates for all classes on the 2moons, CAS-YNU-MHAD and USAA datasets respectively. Reported numbers denote the mean recognition accuracy with five run experiments in percent. The y-axis denotes the mean recognition accuracy over all categories for GCN, MRDGCN-1 and MRDGCN model. The x-axis denotes the number of labeled samples.

<table>
<thead>
<tr>
<th>Method</th>
<th>Citeseer (120)</th>
<th>Cora (140)</th>
</tr>
</thead>
<tbody>
<tr>
<td>ManiReg</td>
<td>60.1</td>
<td>59.5</td>
</tr>
<tr>
<td>SemiEmb</td>
<td>59.6</td>
<td>59</td>
</tr>
<tr>
<td>DeepWalk</td>
<td>43.2</td>
<td>67.2</td>
</tr>
<tr>
<td>Chebyshev ($K = 2$)</td>
<td>53.6</td>
<td>45.8</td>
</tr>
<tr>
<td>Chebyshev ($K = 3$)</td>
<td>53.7</td>
<td>50.5</td>
</tr>
<tr>
<td>GCN</td>
<td>52.8</td>
<td>57.2</td>
</tr>
<tr>
<td>MLP</td>
<td>46.5</td>
<td>55.1</td>
</tr>
<tr>
<td>MRDGCN</td>
<td>66.6</td>
<td>64.8</td>
</tr>
</tbody>
</table>
samples randomly chose from training samples. From Figs. 2–4, we can find that the proposed MRDGCN achieves a higher recognition rate than other models, especially only a few labeled samples. In addition, it also reveals the effectiveness of optimization method for each convolution layer formulation.

Fig. 5 reveals the mean recognition rate of the 2moons database about the label $+1$ (moon images). Fig. 6 shows the mean recognition rate of the CAS-YNU-MHAD database over some human actions, such as jumping forward, jumping up, walking quickly and lying down. Fig. 7 shows the average classification accuracy of the USAA database over some human actions, such as graduation party, non-music performance, parade and wedding dance. The y-axis is the mean recognition rate of each class on different datasets. Each subfigure corresponds one human action. From the results of the human activity datasets, we can see that MRDGCN also gets the best classification performance.

To further demonstrate the effectiveness of dynamic graph structure learning method and the optimization of convolution layer formulation, we compare many state-of-the-art semi-supervised learning algorithms. In addition, we report the mean classification performance under the CAS-YNU-MHAD and 2moons datasets with the 30% and 5% labeled samples respectively. From Figs. 2–7 and Table 2, we can find that our proposed MRDGCN shows the best classification performance. Due to the generalization of the proposed convolution rule Eq. (9) on different datasets, MRDGCN-1 can acquire the optimal static data structure information and effective sample features compared with GCN. Compared with MRDGCN-1 and other semi-supervised learning methods, MRDGCN can get the optimal dynamic space structure information of each layer by the effective combination of our proposed convolution rule Eq. (9) and objective function with manifold regularization term Eq. (4). Finally, MRDGCN can extract more reasonable and effective data features via the convolution fusion of the acquired data structure relationships and input data features. These data indicates that MRDGCN can better preserve and utilize the local manifold structure of data during the training process of model.

4.5. Parameters sensitivity analysis

In our proposed MRDGCN, there exists one parameter $\beta$ to balance the cross entropy loss value and manifold regularization term.
in the objective function. Thus, we conduct extensive experiments to analyze the sensitivity of the parameter $b$. We run MRDGCN with different $b$ values (from 0.0001 to 0.05) and give its mean average recognition accuracy under 30\% and 10\% labeled samples of the CAS-YNU-MHAD and 2moons. As shown in Fig. 8, we can see that when $b$ varies from 0.001 to 0.05, the proposed method has a stable classification performance. It indicates that MRDGCN is less sensitive to the selection of parameter $b$.

5. Discussions

In the future works, we will explore the graph manifold regularization method to maintain the local invariance constraint between data, and then propose the manifold regularization based graph convolutional networks (MRGCN) model. By the combination of our proposed objective function variant Eq.(11) and the effective convolution layer rule of GCN [26], MRDGCN can better utilize the adjacency relationships between data compared with GCN [26]. Thus, under utilizing the static structure relationships between samples, how to choose appropriate objective function to acquire the effective parameters is vital. In other words, MRGCN still cannot optimize the structure relationships between samples.

\[
C(W) = C_1(W) + bC_2(W) = -y\log Y + b\text{tr} \left(Y^TMY\right)
\]

(11)

6. Conclusion

In recent years, deep learning-based graph structure learning models, especially graph convolutional networks (GCN), have captured widespread attention of researchers in data representation learning area with complex structure. Nevertheless, existing GCN

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**Table 2**

Comparison of the different algorithms on human activity datasets.

<table>
<thead>
<tr>
<th>Method</th>
<th>2moons (5%)</th>
<th>CAS-YNU-MHAD (30%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Chebyshev ($K = 2$)</td>
<td>78.8</td>
<td>47.9</td>
</tr>
<tr>
<td>Chebyshev ($K = 3$)</td>
<td>79.2</td>
<td>51.5</td>
</tr>
<tr>
<td>GCN</td>
<td>79.6</td>
<td>38.5</td>
</tr>
<tr>
<td>GAT</td>
<td>80</td>
<td>48.8</td>
</tr>
<tr>
<td>HyperGCN</td>
<td>80.4</td>
<td>47</td>
</tr>
<tr>
<td>HlLapGCN</td>
<td>80.8</td>
<td>49</td>
</tr>
<tr>
<td>MRDGCN</td>
<td>81.6</td>
<td>60.5</td>
</tr>
</tbody>
</table>
and its variants only utilized a static manifold distribution information of samples by spectral convolution operation and give little attention to its optimization problem. Thus, how to preserve and optimize the manifold structure of data still is a challenging problem. In this paper, we present a dynamic GCN model (MRDGCN) for human activity recognition and citation networks classification by combining the traditional manifold regularization model. During the training process, we employ the alternative solution method to learn the optimal filter parameter and structure information, leading to a dynamic graph structure learning model. In addition, we further make a generalization for the layer-wise propagation rule of GCN, and then MRDGCN can extract richer sample features. Substantial experiment results on human activity datasets including CAS-YNU-MHAD, 2moons, USAA and citation networks datasets demonstrate that MRDGCN model outperforms the typical GCN.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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References

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